

Name _____

EE 2240

Exam #1

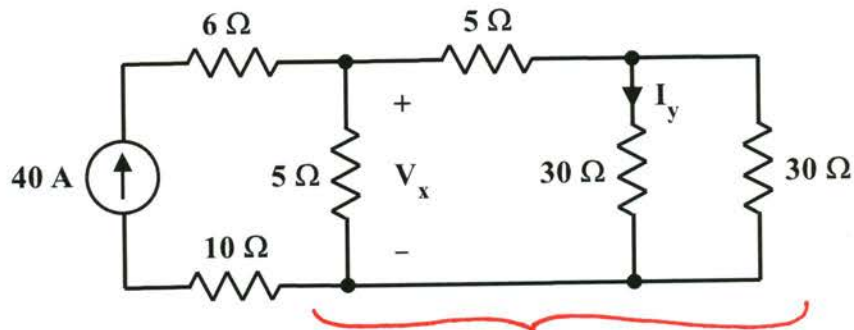
Friday, February 03, 2017

LIBR B07/B16 and TAB 115, 9:00AM – 9:50AM

[closed book – one two-sided 8½"×11" page of notes and calculator allowed, nothing else]

Work must be shown in a neat and orderly fashion if you expect to receive partial credit.

1. Determine the value of V_x and the value of I_y .

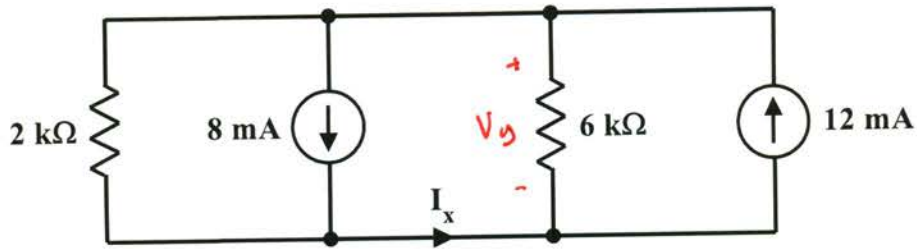


$$\begin{aligned} R_{eq} &= 5\Omega \parallel [5\Omega + (30\Omega \parallel 30\Omega)] \\ &= 5\Omega \parallel [5\Omega + 15\Omega] \\ &= 5\Omega \parallel 20\Omega \\ &= 4\Omega \end{aligned}$$

$$V_x = 40\text{A} \times R_{eq} = 160\text{V}$$

$$I_y = \frac{1}{2} \cdot \frac{V_x}{20\Omega} = 4\text{A}$$

2. Determine the value of I_x and the amount of power absorbed by the $2\text{ k}\Omega$ resistor.

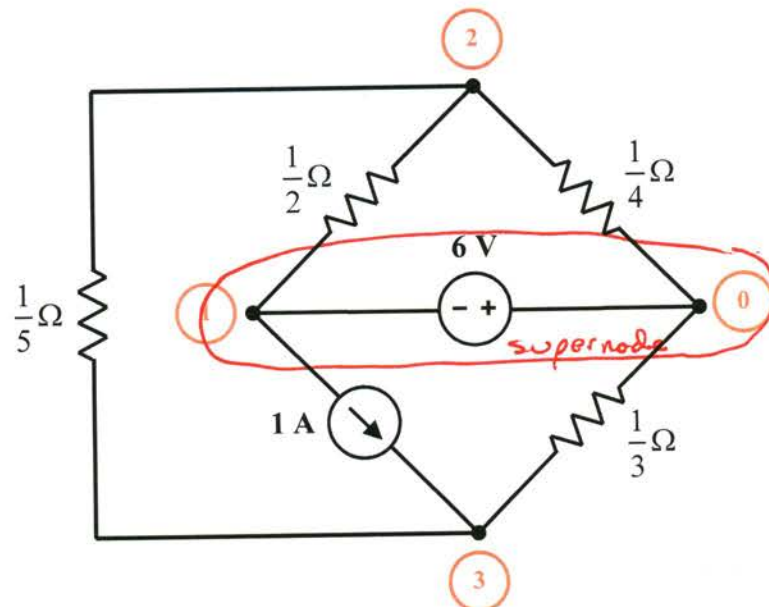


$$V_y = (2\text{ k}\Omega \parallel 6\text{ k}\Omega) \cdot (12\text{ mA} - 8\text{ mA})$$
$$= 6\text{ V}$$

$$I_x = 12\text{ mA} - \frac{V_y}{6\text{ k}\Omega} = 12\text{ mA} - \frac{6\text{ V}}{6\text{ k}\Omega} = 11\text{ mA}$$

$$P_{2\text{ k}\Omega} = \frac{V_y^2}{2\text{ k}\Omega} = \frac{(6\text{ V})^2}{2\text{ k}\Omega} = 18\text{ mW}$$

3. Use the method discussed in class to determine a set of node equations describing the circuit shown, and express them in the standard matrix form. Use the node labels that are already assigned. *Do not attempt to solve the equations.*



$$V_1 = -6V \quad (\text{constraint equation from the supernode})$$

$$\frac{V_2 - V_3}{\left(\frac{1}{5}\right)} + \frac{V_2 - V_1}{\left(\frac{1}{2}\right)} + \frac{V_2}{\left(\frac{1}{4}\right)} = 0 \quad (\text{KCL at node 2})$$

$$\frac{V_3 - V_2}{\left(\frac{1}{5}\right)} - 1 + \frac{V_3}{\left(\frac{1}{3}\right)} = 0 \quad (\text{KCL at node 3})$$

In matrix form:

$$\begin{bmatrix} 1 & 0 & 0 \\ -2 & 11 & -5 \\ 0 & -5 & 8 \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \\ V_3 \end{bmatrix} = \begin{bmatrix} -6 \\ 0 \\ 1 \end{bmatrix}$$

4. Solve for the value of z . Check your work; there will be very little partial credit on this problem.

$$\begin{bmatrix} 1 & 0 & 0 \\ -2 & 11 & 5 \\ 0 & -5 & 8 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \\ -113 \end{bmatrix}$$

From rows 1 and 2:

$$11y + 5z = 0$$

Multiply this by 5:

$$55y + 25z = 0$$

Multiply the third row by 11:

$$-55y + 88z = -1243$$

Add these last two together:

$$113z = -1243$$

$$\Rightarrow z = -11$$